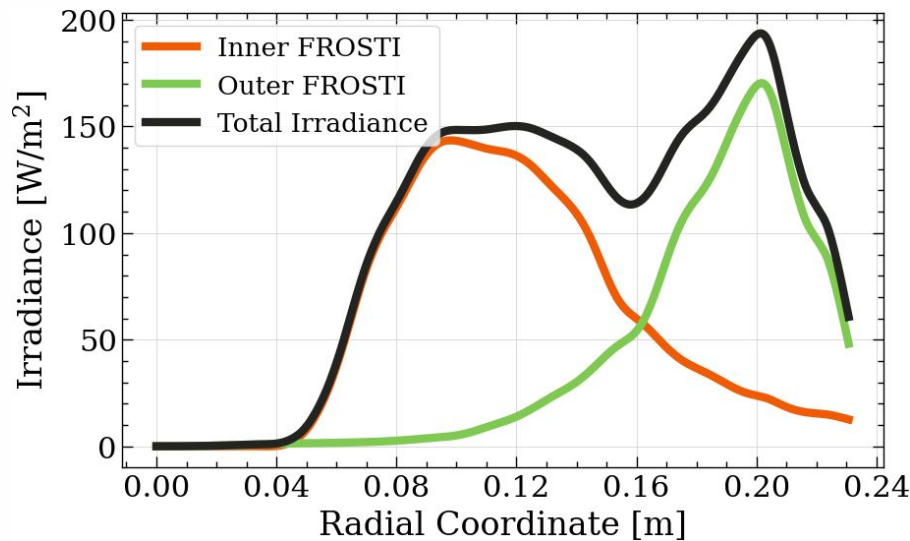
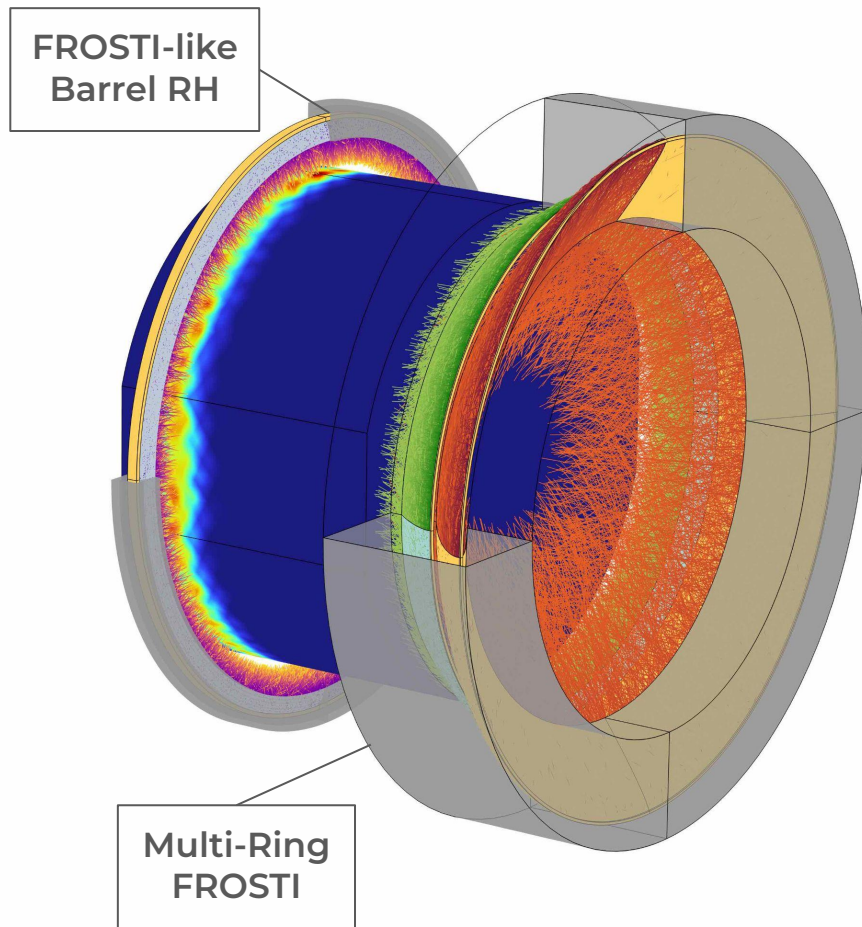
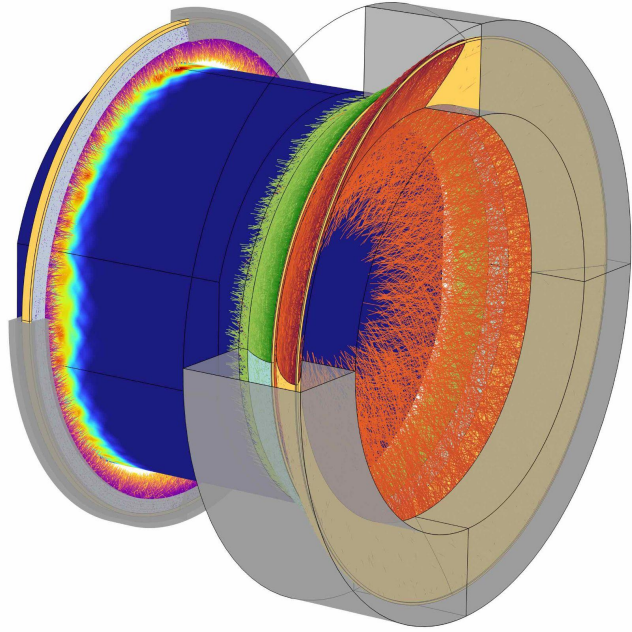


# Multi-Ring FROSTI for Finer Actuation



Complex total irradiance profile  
→ more precisely targeted  
wavefront corrections for A#

# Multi-Ring FROSTI Design for A<sup>#</sup> and CE



Design parameter  
space optimization

To minimize both the surface and subtract wavefront RMSE, with at least two FROSTI-like heater rings, we have

1. Width, location and individual power for each irradiance ring,  $\text{DoF}=2*3=6$ ;
2. Ring heater power,  $\text{DoF}=1$ ;
3. In total **7D** parameter space exploration.

Geometric param:

1. Width
2. location

Optimization **One**

Power param:

1. FROSTI power
2. RH power

Optimization **Two**

Nested loop

For each step in optimization loop **one**, we need to run an FEA model over the width and locations.

# Laguerre-Based Surrogate Optimization

Laguerre decomposition:

1. You only compute once.
2. No need to simulate FEA model at **every** step.

Geometric param:

1. Width
2. location

Optimization **One**

Nested loop

Power param:

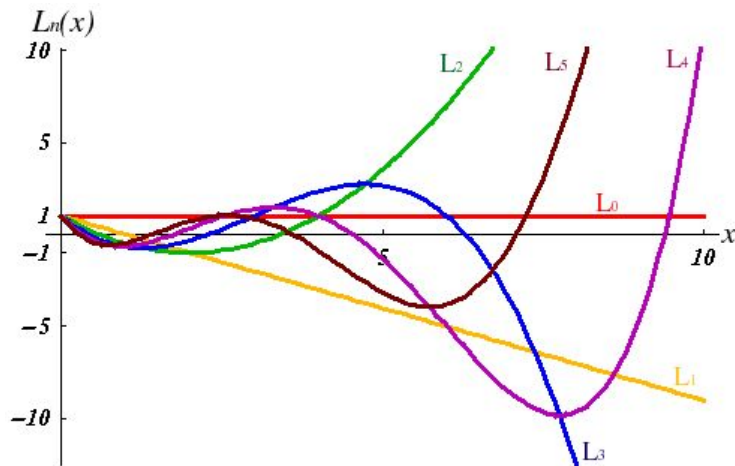
1. FROSTI power
2. RH power

Optimization **Two**

Surrogate model via interpolation/ML for the thermal response over the entire geometric space.

**FEA on the fly → Look up table**

$$\vec{c}_{\text{total}} = \sum_{k=1}^K P_k \cdot \vec{c}(r_{0,k}, \sigma_k) + P_{\text{RH}} \cdot \vec{c}_{\text{ring}}$$



Radially symmetric, Laguerre polynomials, larger  $n \rightarrow$  higher spatial frequency

# Laguerre-Based Surrogate Optimization

Laguerre decomposition:

1. You only compute once.
2. No need to simulate FEA model at **every** step.

Geometric param:

1. Width
2. location

Power param:

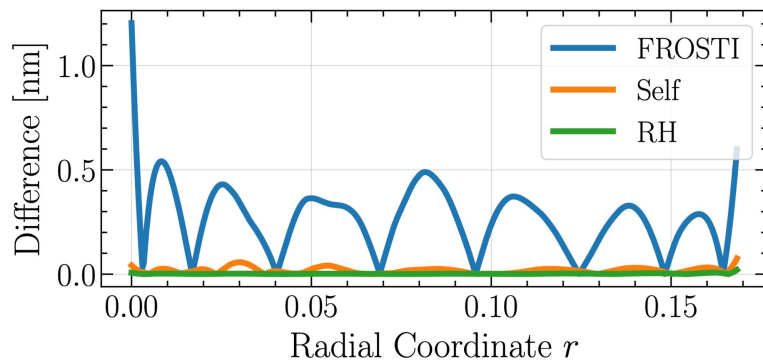
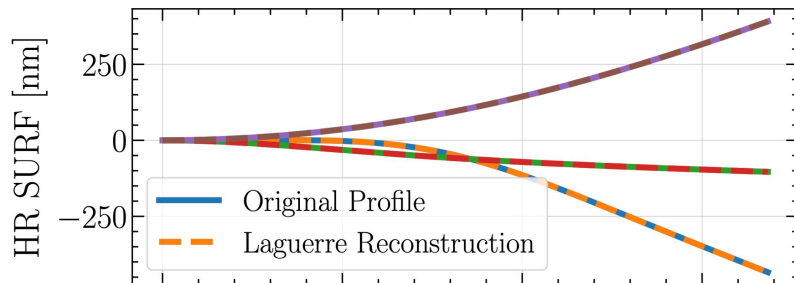
1. FROSTI power
2. RH power

Optimization **One** ↪ Nested loop ↪ Optimization **Two**

Surrogate model via interpolation/ML for the thermal response over the entire geometric space.

**FEA on the fly →→ Look up table**

$$\vec{c}_{\text{total}} = \sum_{k=1}^K P_k \cdot \vec{c}(r_{0,k}, \sigma_k) + P_{\text{RH}} \cdot \vec{c}_{\text{ring}}$$



Example Laguerre decomposition ( $n \leq 10$ ) for the thermal deformation due to FROSTI, Self heating and RH

# Laguerre-Based Surrogate Optimization

Laguerre decomposition:

1. You only compute once.
2. No need to simulate FEA model at **every** step.

Benefit of this approach:

1. Less computation time and much more efficient parameter search.
2. More flexible loss function. E.g. emphasize the suppression of low-order aberrations.

Geometric param:

1. Width
2. location

Power param:

1. FROSTI power
2. RH power

Optimization **One**  Optimization **Two**

Surrogate model via interpolation/ML for the thermal response over the entire geometric space.

**FEA on the fly →→ Look up table**

$$\vec{c}_{\text{total}} = \sum_{k=1}^K P_k \cdot \vec{c}(r_{0,k}, \sigma_k) + P_{\text{RH}} \cdot \vec{c}_{\text{ring}}$$

$$\mathcal{L}_{\text{total}} = \mathcal{L}_E + \beta \mathcal{L}_{\text{RMS}}$$

$$\mathcal{L}_E(\{r_{0,k}, \sigma_k, P_k\}, P_{\text{RH}}) = \sum_{n=0}^{N-1} w_n \cdot (c_{\text{res},n})^2$$

$$\mathcal{L}_{\text{RMS}} = \sqrt{\int_0^R [h_{\text{res}}(r)]^2 r dr}$$